

TABLE 5

ALL POSITIVE INTEGERS NOT REPRESENTED BY
 $a, b, c = ax^2 + by^2 + cz^2$

1, 1, 1	<i>A</i>	1, 5, 8	$4n+3, 8n+2, I$
1, 1, 2	<i>C</i>	1, 5, 10	<i>J</i>
1, 1, 3	<i>D</i>	1, 5, 25	$5n \pm 2, 25n \pm 10, E$
1, 1, 4	$8n+3, A$	1, 5, 40	$4n+3, 8n+2, J$
1, 1, 5	<i>E</i>	1, 6, 6	$8n+3, G$
1, 1, 6	<i>B</i>	1, 6, 9	$3n+2, B$
1, 1, 8	$4n+3, 16n+6, C$	1, 6, 16	$8n \pm 3, 16n \pm 2,$ $64n+8, B$
1, 1, 9	$9n \pm 3, A$		
1, 1, 12	$4n+3, D$	1, 6, 18	$3n+2, 9n+3, K$
1, 1, 16	$8n+6, 4n+3,$ $32n+12, A$	1, 6, 24	$8n \pm 3, 32n+12, G$
1, 1, 21	$D, E, 49^k(49n+7r),$ $r=1, 2, 4$	1, 8, 8	$4n+2, 4n+3,$ $8n+5, A$
1, 1, 24	$4n+3, 8n+6, B$	1, 8, 16	$4n+2, 4n+3,$ $8n+5, C$
1, 2, 2	<i>A</i>	1, 8, 24	$4n+2, 4n+3, K$
1, 2, 3	<i>H</i>	1, 8, 32	$4n+2, 8n+3, A,$ $8n+5, 32n+20$
1, 2, 4	<i>C</i>		
1, 2, 5	<i>I</i>	1, 8, 40	$4n+2, 4n+3,$ $8n+5, 32n+28, F$
1, 2, 6	<i>K</i>		
1, 2, 8	$8n+5, A$	1, 8, 64	$4n+2, 8n+3, C,$ $64n+40,$ $4r(8n+5),$ $4r(8n+7), r=0, 1$
1, 2, 10	$8n+7, F$		
1, 2, 16	$8n+5, 8n+7,$ $16n+10, C$		
1, 2, 32	$16n+14, A,$ $2r(8n+5), r=0,$ 1, 2	1, 9, 9 1, 9, 12 1, 9, 21	$3n+2, 9n \pm 3, A$ $3n+2, 4n+3, D$ $3n+2, D, E,$ $49^k(49n+7r),$ $r=1, 2, 4$
1, 3, 3	<i>G</i>		
1, 3, 4	$4n+2, D$		
1, 3, 6	$3n+2, C$	1, 9, 24	$3n+2, 4n+3,$ $8n+6, B$
1, 3, 9	$3n+2, D$		
1, 3, 10	$D, F, 4^k(16n+2)$	1, 10, 30	<i>D, J, K</i>
1, 3, 12	$4n+2, G$	1, 12, 12	$4n+2, 4n+3, G$
1, 3, 18	$3n+2, 9n+6, H$	1, 12, 36	$3n+2, 4n+2,$ $4n+3, D$
1, 3, 30	$G, I, 4^k(16n+6)$		
1, 3, 36	$3n+2, 4n+2, D$	1, 16, 16	$4n+2, 4n+3, A,$ $8n+5, 16n+8,$ $16n+12$
1, 4, 4	$4n+2, 4n+3, A$		
1, 4, 6	$16n+2, B$		
1, 4, 8	$4n+2, 4n+3, C$	1, 16, 24	$4n+2, 4n+3, B,$ $8n+5, 64n+8$
1, 4, 12	$4n+2, 4n+3, D$		
1, 4, 16	$4n+2, 4n+3,$ $16n+12, A$	1, 16, 48	$4n+2, 4n+3, 8n+5,$ $16n+8, 16n+12,$ <i>D</i>
1, 4, 24	$4n+2, 4n+3, B$		
1, 4, 36	$4n+2, 4n+3,$ $9n \pm 3, A$	1, 21, 21	<i>A, G, 49^k(7n+r), $r=3, 5, 6$</i>
1, 5, 5	$5n \pm 2, A$		

TABLE 5—Continued

1, 24, 24	$4n+2, 4n+3, G,$ $8n+5, 32n+12$	3, 4, 36	$3n+2, 4n+1,$ $4n+2, D$
1, 24, 72	$3n+2, 4n+2, K,$ $4n+3, 9n+3$	3, 7, 7	$D, K, 49^k(7n+r),$ $r=1, 2, 4$
1, 40, 120	$4n+2, 4n+3, D,$ <i>J, K</i>	3, 7, 63	$3n+2, D, K,$ $49^k(7n+r), r=1,$ $2, 4$
1, 48, 144	$3n+2, 8n+5, D,$ $4r(4n+2),$ $4r(4n+3), r=0, 1$	3, 8, 8	$4n+1, 4n+2, D,$ $8n+7, 32n+4$
2, 2, 3	$8n+1, D$	3, 8, 12	$4n+1, 4n+2, L$
2, 3, 3	<i>L</i>	3, 8, 24	$3n+1, 4n+1,$ $4n+2, A$
2, 3, 6	$3n+1, A$		
2, 3, 8	$8n \pm 1, 32n+4, D$	3, 8, 48	$4n+1, 4n+2, L,$ $8n+7, 64n+24$
2, 3, 9	$3n+1, 9n+6, H$		
2, 3, 12	$16n+6, L$	3, 8, 72	$3n+1, 4n+1, 4n+2,$ $8n+7, 32n+4, D$
2, 3, 18	$3n+1, 8n+1, D$		
2, 3, 48	$8n+1, 16n \pm 6,$ $64n+24, L$	3, 10, 30	A, G, N'
2, 5, 6	<i>B, I, M</i>	3, 16, 48	$4n+1, 4n+2, 8n+7,$ $16n+4, 16n+8, G$
2, 5, 10	$8n+3, N$	3, 40, 120	$4n+1, 4n+2, A,$ <i>G, N</i>
2, 5, 15	<i>B, H, N</i>		
2, 6, 9	$3n+1, 9n+3, K$	5, 6, 15	C, J, L
2, 6, 15	<i>E, F, L</i>	5, 8, 24	$4n+2, 4n+3, B,$ <i>I, M</i>
3, 3, 4	$4n+1, G$		
3, 3, 7	$G, M, 49^k(49n+7r),$ $r=3, 5, 6$	5, 8, 40	$4n+2, 4n+3, N,$ $8n+1, 32n+12$
3, 3, 8	$4n+1, 8n+2, L$	8, 9, 24	$3n+1, 4n+2, K,$ $4n+3, 9n+3$
3, 4, 4	$4n+1, 4n+2, D$		
3, 4, 12	$4n+1, 4n+2, G$	8, 15, 24	$4n+1, 4n+2, B,$ <i>F, L</i>

Diagonal

Table 5 gives each of the 102 regular forms and all the positive integers not represented by it. Use will be made of the abbreviations

$$\begin{aligned}
 A &= 4^k(8n+7), & B &= 9^k(9n+3), \\
 C &= 4^k(16n+14), & D &= 9^k(9n+6), \\
 E &= 4^k(8n+3), & F &= 25^k(25n \pm 5), \\
 G &= 9^k(3n+2), & H &= 4^k(16n+10), \\
 I &= 25^k(25n \pm 10), & J &= 25^k(5n \pm 2), \\
 K &= 4^k(8n+5), & L &= 9^k(3n+1), \\
 M &= 4^k(8n+1), & N &= 25^k(5n \pm 1).
 \end{aligned}$$