

Name: _____

Please show all work and justify your answers.

1. Let $a, b \in \mathbf{N}$. Prove that $\text{lcm}(a, b)$ divides any common multiple of a and b .
2. Sketch the subgroup lattice for \mathbf{Z}_{45} .
3. Prove that any nontrivial finite group has an element of prime order.
4. If G is a group, $a \in G$, and $|a| = 24$, prove that there exists $b \in G$ such that $b^5 = a$.

1	2	3	4	total (40)