

Calculus I, MAT 1214 (2-5)
Midterm, March 8, 1995
Instructor: D. Gokhman

Name: _____

1. (30 pts.) Find the following limits (show work):

(a) $\lim_{x \rightarrow 0} \frac{x}{\tan(x)}$ (b) $\lim_{x \rightarrow 0^-} \frac{2x + |x|}{|x|}$ (c) $\lim_{x \rightarrow 0} x \cos\left(\frac{1}{x^2}\right)$

2. (30 pts.) Differentiate each of the following functions:

(a) $x^2 \sin^2(x^2)$ (b) $\frac{3x}{x^2 + 1}$ (c) $\sqrt{\cos(x)}$

3. (20 pts.) Find an equation for the line that is perpendicular to the graph of $y = x^2$ and passes through the point $(-3, 0)$.
4. (30 pts.) Find the critical points of the function $f(x) = 3x^4 + 8x^3 - 18x^2 + 100$. Find the minimum and maximum values of this function in the interval $[0, 2]$.

| 1 | 2 | 3 | 4 | total (110) |
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